The Role of Invariants
in an Automatic Program Verifier

Myia Archer
Code 5546, Naval Research Laboratory,
Washington, DC 20375
archer@itd.nrl.navy.mil

Abstract. Invariants are central to establishing correctness of programs.
Thus, a large part of an automatic program verifier needs to be autom-
nated support for verifying program invariants. This paper discusses
where the invariants come from, what can be involved in establishing
that they hold, and the extent to which the process of finding and prov-
ing invariants can be automated. The paper also discusses several chal-
 lenges related to establishing invariants and other correctness properties
of programs that, if addressed, would make the feedback produced by a
verifying compiler more clearly meaningful and understandable in terms
of the global behavior of programs.

1 Introduction

In undertaking to construct and exploit an automatic program verifier, one must
first focus in on the problems to be solved. There are several natural questions
that arise, e.g.:

– What does it mean to verify a program?
– What does it mean for a program to be correct?
– Assuming program verification involves proving a set of properties:
  • What types of properties are to be established?
  • Where do the properties come from?
  • Are the properties capable of automatic proof?
– Finally, what support should be provided by the automatic program verifier
to allow a user to best exploit it?

This paper will explore these issues, and will argue that one major problem on
which to focus is the automation of invariant proofs. This paper will also take
note of several challenges related to establishing invariants and other correctness
properties of programs, and suggest that the notion of a verifying compiler as a
grand challenge be given a broad scope.

Sections 2 through 5 discuss the questions listed above, Section 6 discusses
related challenges. Finally, Section 7 presents some conclusions and discusses our
current and future research that relates to some of the challenges.
2 What does it mean to verify a program?

Since the seminal work in [11] and [6], program verification is often thought of in terms of assertions that can be proved to hold at various points in the program. In particular, for programs designed to run to completion while performing some computation, assertions at the beginning and end of the program can be used to define the expected result of the computation. The approach is also valid for programs that run indefinitely; in this case, assertions (about input and output streams) before reads and after writes can be used to define the expected visible behavior of the program.

However, certain programs intended to run indefinitely are better specified by giving an operational model, usually accompanied by invariant properties of the model. This is the approach used, for example, in SCR [12], TIOA [18] and other software development tools. What then needs to be established of the program is that it refines the specification. This approach can be thought of as model-based verification.

To many, verification means another form of model-based verification: model checking. Model checking has been used more often in the context of hardware verification than software verification, but recent advances such as automated abstraction refinement (see, e.g., [7]) have extended its applicability to software. The use of model checking for verification implies a specific set of properties to be checked.

3 What does it mean for a program to be correct?

As discussed in Section 2, the term “program verification” in any sense means establishing that the program has certain properties. These properties may be defined by assertions associated with various points in the program, a model to which the program must conform, or other assertions about the program as a whole (such as liveness, or absence of deadlock or livelock).

For some programs, what is needed for correctness is clear. For example, a program that sorts a list needs to take a list as input and produce a sorted version of the list as output. In model-based verification, one establishes a relationship (such as refinement or simulation) between a program and a model, and proves properties of the model, which can then be interpreted in terms of program properties. In tools such as SCR and TIOA, conformance to the model may be the primary criterion for correctness. However, in model checking, the model is usually created to establish a property of the program. With model checking, and to some extent in any type of model-based verification, a major question with respect to correctness is whether the set of models representing properties to be established does in fact capture the desired behavior of the program.

There are many cases in which it may not be feasible to establish the full desired behavior, i.e., the complete functional correctness, of a program, although one would like at least to establish certain specific properties of the program, e.g., security properties. For such cases, model-based verification is especially appropriate.
For a very complex program, e.g., a graphical editor, the definition of correctness is equally complex, and it can even be unclear what correctness means precisely. For such programs, one may be most interested in "good" behavior from the user’s and operating system’s point of view: Will the program terminate unexpectedly due to a segmentation fault? Are there possible buffer overflows or deadlocks? Capturing most of these properties as program assertions is straightforward.

4 Properties: formulation and proof

4.1 What types of properties are to be established?

All the correctness properties mentioned above can be formulated as invariants of some state machine. The simplest category from the point of view of proof is the state invariants: program assertions, absence of deadlock, and many specified properties of models fall in this category. Conformance to a model can also be cast as a state invariant of a composition automaton (representing composition of the model and the program). Almost as simple are safety properties, which involve at most a bounded sequence of transitions. More difficult to prove are liveness properties, which can involve reasoning about an unbounded sequence of states and may involve some fairness assumptions.

4.2 Where do the properties come from?

In the interest of separation of concerns, one can assume, in tackling the challenge of building an automatic program verifier, that the properties that must be established of the program are given. However, it is clear that an automatic verifier will not be much help in establishing program correctness if properties that imply its correctness have not been formulated by someone. Thus, a related challenge is to persuade developers (or other stakeholders in a piece of software) to specify in some form what the software is to do. A further related challenge is to create a tool that, given appropriate information, can derive assertions about a program to be used by an automatic program verifier from assertions about an abstract model of the program’s behavior.

In the context of asserted programs, there has been some work [10] on dynamically discovering likely program invariants that could produce some of the needed assertions in a program (which would then be subject to proof). There has also been work on generating known invariants, starting from [8] and [9], which consider program assertions. Later work includes [13], which also considers program assertions, and [15], which considers invariant properties of specifications. Although these approaches can help furnish some of the assertions, the connection between the assertions and program correctness would need to be established by someone who understands what the program is supposed to do, or how a model is supposed to behave. Creating automated support for generating program assertions from assertions about a model appears to be an open problem.
4.3 Are the properties capable of automatic proof?

Some program assertions can be established without induction: e.g., input assertions can be assumptions, other assertions can be established through weakest precondition computations, and further assertions can be established from existing ones by the application of decision procedures. A challenge in this connection is to develop additional decision procedures to be integrated into existing ones that can handle data types (beyond numerical, boolean, and enumerated types) for which many assertions are decidable.

However, for certain classes of assertions, induction is required. For example, induction is generally needed to establish loop invariants. Induction is also generally needed to establish liveliness properties. For a finite model, one can sometimes avoid induction: properties of finite models can (if state explosion is manageable) be established by exhaustive search (model checking). However, establishing invariant properties of infinite (and sometimes, very large finite) models requires theorem proving and, typically, induction.

Thus, even though some program properties can be established by other means, a general truly automatic program verifier would need to be able to do induction proofs automatically. A completely general approach to doing this is not possible, because the general problem of establishing whether an assertion is an invariant is undecidable. In principle, provided the base and induction cases can be stated in first-order logic, valid invariants can be established by induction automatically. However, efficiency is an issue; so is the problem that some properties being checked are false—as may be the case for the induction step when one is trying to prove a possibly true invariant by proving that it is inductive. In particular, proofs by induction of invariants also often require strengthening of the invariants, a process that is not always automatable. Strengthening can be automated, to a degree, as has been illustrated in SCR. Note that an equivalent approach to strengthening is the introduction of additional invariants as lemmas. In the context of SCR, it has been possible to create an induction proof strategy that uses automatically generated invariants [15] as lemmas and that proves many properties of SCR specifications automatically; see, e.g., [14].

Thus, automating induction proofs of program properties is itself a challenge. The goal would be to create a technique that would cover the kinds of assertions that normally arise in practice. Techniques such as proof planning with rippling [5, 4] have had some success, but are still not universal.

Mechanical proofs—by induction or otherwise—of correctness properties of abstract models are often best constructed interactively. This is because for abstract models, correctness properties can contain quite complex predicates (e.g., the authenticated predicate in the basic TESLA model in [2] involves existential quantifiers and is recursively defined) and are potentially higher-order. As shown by our experience with TAME [3], efficient interactive construction of proofs can be made more feasible if an appropriate special domain tool or prover interface is provided. (TAME is discussed further in Section 5, and in more detail in Section 7.)
5 How to exploit an automatic program verifier?

As has been noted above, an automatic verifier presupposes some form of specification against which to verify the program. A user better equipped to specify is thus better equipped to verify. But such a user is also better equipped to test. To state the obvious: the user should test the assertions before using the program verifier, because verification is expensive; only after one has evidence that a set of properties is likely correct should one undertake to prove the properties. Thus, a program verifier is best used in conjunction with a testing tool.

Equally important to knowing that a program has certain properties is knowing why it has those properties. For example, one usually does not want a property to be vacuously true, as might happen (in a program) for the postcondition of an intentionally nonterminating loop, or (in a model) when all preconditions of transitions are false. Thus, in addition being able to prove properties, it is desirable for the verifier to produce some degree of proof explanation. A variety of theorem proving techniques provide some form of explanation. Several automatic proof techniques provide proof explanation; examples include ACL2 [16, 17] and approaches based on proof planning such as [19]. Our tool TAME [3] provides explanations for invariant proofs produced with interactive guidance.

However, explanations are produced, the same techniques used in proof explanation can be adapted to provide some explanation of proof failure—i.e., what point and proof goal did the proof reach when the automatic verifier was unable to continue? When the automatic verifier is unable to verify a program, the next action needs to be either modification of the program or modification of the specification. While performing the proper corrective action is an art form, feedback from the automatic verifier is an important prerequisite to making the correction.

Addressing some other challenges related to the automatic program verifier would allow the automatic verifier to be exploited as fully as possible. The next section discusses these challenges and notes how addressing them would help.

6 Related challenges

As noted above, the challenge of building an automatic invariant prover is a part of the challenge of building an automatic program verifier. The challenge of improving and expanding the scope of decision procedures also falls into this category. But there are other challenges that, if addressed, would increase the usefulness of an automatic verifier. Two have already been mentioned.

First, it would be helpful if software developers could be convinced to provide some form of specification of what the software is supposed to do. With respect to low level specification, this is not an unreasonable hope: for example, the inclusion of assertions with C and Java code is provided for and beginning to come into practice. It is likely unrealistic to hope that all software developers will provide operational specifications that capture the intended behavior of the code. However, when the correctness of the code is essential, such specifications are
more likely to be developed. One way of establishing that a program refines an operational specification is to relate assertions in the specification (e.g., pre- and post-conditions associated with transitions) to assertions in the code. Thus, in cases where an operational specification is available, there is a second challenge: automating the mapping of assertions in the specification to assertions in the code, based on information provided by the user that relates program states to abstract (specification-level) states and program segments to transitions in the specification.

A third, further challenge is to develop methods that can be applied by developers in designing programs for verifiability, and induce the developers to use them, While some such guidance already exists (e.g., avoid certain constructs), this guidance is mostly of a "local" nature. An open question is whether guidance can be provided for structuring programs so that particular properties (e.g., for security, separation of data) are easier to establish.

Addressing these challenges would help ensure first, that the automatic program verifier is proving properties of interest and second, that the automatic verifier's task is made as simple as possible.

7 Conclusions and Plans for the Future

A verifying compiler that verifies assertions in programs is only part of the answer to the problem of producing verifiably correct programs. The challenge of building an automatic program verifier can be conceived more generally as covering not only a verifier of assertions in programs but a verifier (perhaps interactive) that a program conforms to a model. For either the program-assertion-based or model-based verification style, the automation of proofs of invariants, and in particular induction proofs, will play central role.

This paper has identified several related challenges to be met; some of them are directly implied by the challenge of building an automatic program verifier. Others are associated with additional parts of the process of establishing correctness properties of programs. Because addressing these others will increase the effectiveness of the automatic program verifier, it is worth considering including them as part of the overall challenge. Below is a summary of our current and future work that does (or will) address some of the related challenges.

Two of the challenges identified above are addressed to some degree for model-based verification by the tool TAME (Timed Automata Modeling Environment) [1, 3], a specialized interface to PVS [23] for proving properties of timed I/O automata [20, 21]. In particular, TAME attempts to make specification of models easier. It also partially automates proofs of invariants, including state invariants, transition invariants, and abstraction properties such as refinement and forward simulation [22] by providing a set of high level proof steps that allow a proof sketch to be mechanically checked. For SCR specifications, TAME can prove many invariant properties automatically. TAME provides user feedback for failed proofs both inside the prover at the point of a proof dead end and in saved TAME proofs through structure, proof step names, and com-
ments. A prototype proof tool that translates TAME proofs into English has been implemented. Work is continuing on improving TAME in all these areas.

It is also planned to extend the work on TAME by increasing the degree to which proofs of invariants can be automated. This will be done by 1) developing techniques that can prove more invariants automatically by building on previously proved invariants, finding alternative, useful instantiations of the inductive hypothesis, and so on; and 2) exploring the possible use of techniques such as rippling in proving invariants of TAME models.

Other plans for the near future include:

- The use TAME or a similar “special domain” PVS interface to model some medium-sized programs and establish their correctness. The goal is to build on the techniques used in TAME to permit program verification on a level nearer to the level of program assertions.

- Development of automated support for translating assertions at the model level into assertions at the program level.

Some interesting lessons, and perhaps some new associated challenges, are likely to result from these efforts.

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References


